

1 **Astronomically forced climate change in the late Cambrian**

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13

14 **Abstract**

15 We report evidence for Milankovitch cycles in two drill cores from the Cambro–Ordovician Alum
16 Shale Formation of Scandinavia. The signal is preserved in elemental abundances recorded at high
17 stratigraphic resolution by core scanning XRF analysis (0.2 mm resolution). The new data enable us
18 to establish a floating timeline calibrated to the stable 405 kyr eccentricity cycle for a ~8.7 Myr
19 interval across the Miaolingian–Furongian boundary. This interval spans the Steptoean Positive
20 Carbon Isotope Excursion (SPICE), which is recorded in the $\delta^{13}\text{C}_{\text{org}}$ in the studied drill cores. We
21 calculate the durations of the *Olenus* Superzone to 3.4 ± 0.2 Myr, the *Parabolina* Superzone to 1.9
22 ± 0.3 Myr, the *Leptoplastus* Superzone to 0.33 ± 0.18 Myr, the *Protopeltura* Superzone to $0.51 \pm$
23 0.20 Myr, and the SPICE event straddling the Paibian and lower main part of the Jiangshanian
24 Stage to 3.0 ± 0.2 Myr. The sedimentation rate shows similar trends at both drilling locations and is
25 inversely correlated to eustatic sea level changes in certain time intervals, opening tantalizing new
26 prospects of using cyclostratigraphic analyses of shales to track eustatic sea level variations. The
27 identification of obliquity cycles enables us to calculate the Cambrian Earth–Moon distance as well
28 as the day length at ~493 Ma to $368.9 \pm 2.3 \cdot 10^6$ m and 21.78 ± 0.29 hours, respectively.

29

30 **Keywords:** Cyclostratigraphy, Core Scanning XRF, Alum Shale, SPICE event, Earth–Moon
31 distance, Furongian

32

33 **1. Introduction**

34

35 The Cambrian was characterized by a warm “greenhouse” climate with seawater temperatures
36 exceeding 30°C in the tropics, 20–25°C at ~65–70°S, and ~15°C at the poles with no sea ice or
37 continental ice sheets on the South Polar continent (Hearing et al., 2018; Wotte et al., 2019).

38 Nevertheless, evidence of rapid and dramatic sea level changes have been interpreted in the context
39 of glacio-eustasy, since ice-albedo feedbacks are known to be powerful amplifiers of astronomical
40 insolation forcing (Babcock et al., 2015). A long-term sea level rise of at least 200 m occurred
41 through the Cambrian while Laurentia, Baltica, Siberia and Avalonia separated and drifted away
42 from Gondwana (Peng et al., 2012). Baltica – in focus in the present study – was located at mid
43 southerly latitudes (Fig. 1A).

44 The Cambrian marks an important phase in the history of life on Earth, with rapid
45 evolution of the marine animal ecosystems. The period was also characterized by several major
46 changes in the Earth’s carbon cycle that are expressed in carbon isotope excursion events (Bambach
47 et al., 2004; Peng et al., 2012). One of these events is the Steptoean Positive Carbon Isotope
48 Excursion (SPICE) recorded in the early Furongian (late Cambrian) by a large positive shift in the
49 $^{13}\text{C}/^{12}\text{C}$ ratio in marine sedimentary successions worldwide (Saltzman et al., 2000). The SPICE
50 event was associated with a large disturbance in the global marine cycles of sulfur, molybdenum
51 and uranium, suggesting an extensive expansion of marine anoxia in the oceans (Gill et al., 2011;
52 Dahl et al., 2014).

53 The Cambrian timeframe is constrained by only a few radiometric ages that can be
54 more or less reliably correlated to cosmopolitan stage boundaries (Ogg et al., 2016). The
55 Miaolingian (Cambrian global stages 5–7, ~509 – 497 Ma) and Furongian (Cambrian stages 8–10,
56 ~497–485.4±1.9 Ma) together straddle approximately 24 Myr and 20–30 agnostid trilobite biozones

57 (not all global) (Peng et al., 2012; Ogg et al., 2016). The average durations of the individual stages
58 can be calculated by linear interpolation, assuming each biozone represents an equal length of time
59 (Peng et al., 2012). However, this assumption is almost certainly wrong. Thus, a fundamental
60 motivation for this study is to improve the temporal framework for the late Cambrian and across the
61 SPICE event. This will pave the way for a better understanding of the trigger and dynamic
62 feedbacks at play during this biogeochemical event.

63 The identification of astronomically forced climate cycles expressed in sedimentary
64 successions can be used to refine the temporal resolution of the geological time scale. Once
65 Milankovitch cycles are recognized in the stratigraphic record, they can be used to establish a
66 relative ‘floating’ timescale. This approach has long been applied to Cenozoic and Mesozoic
67 sediments (Hinnov, 2018 and references therein), but recent studies have pushed the method further
68 back into the Paleozoic, e.g. Permian (Wu et al., 2013; Fang et al., 2017), Carboniferous (Davydov
69 et al., 2010), Devonian (De Vleeschouwer et al., 2012; De Vleeschouwer et al., 2015; Ellwood et
70 al., 2015; Da Silva et al., 2016; Pas et al., 2018), Silurian (Gambacorta et al., 2018), Ordovician
71 (Fang et al., 2016), and even into the Proterozoic (e.g. Zhang et al., 2015) and Neoproterozoic (Walker
72 and Zahnle 1986; Hofmann et al., 2004; de Oliveira Carvalho Rodrigues et al., 2019). So far,
73 applications to the Cambrian are limited to only one section covering a ~1.4 Myr interval across the
74 Drumian–Guzhangian boundary in China (Fang et al., 2020), although thick cyclic sequences of
75 shallow marine carbonate platforms are found globally (Derby et al., 2012) and have already been
76 suggested to record astronomically forced sea level oscillations (Osleger & Read, 1991).

77 Cyclostratigraphic tuning relies on accurate astronomical modeling of the planetary
78 orbital motions which becomes challenging prior ~50 Ma (Laskar et al., 2004). The chaotic nature
79 of the Solar System makes it impossible to predict the exact phases and amplitudes of the 100-kyr
80 and 405-kyr eccentricity components beyond ~50 and ~200 Ma, respectively. Nonetheless,

81 modeling and observations suggests that the 405 kyr eccentricity period has been stable throughout
82 Earth's history, making it the prime calibration target for pre-Cenozoic sequences (Laskar et al.,
83 2004). Calibrations combining cyclo- and chronostratigraphy confirm this is the case, and the 405
84 kyr eccentricity period is found to be stable to within ~10% uncertainty as far back as ~1.4 Ga
85 (Zhang et al., 2015). In contrast, the obliquity and precession periods have changed due to the
86 dissipative effects of the Earth–Moon system that result in lunar recession, longer day length,
87 slower obliquity and precession rates of the Earth. Thus, empirical constraints on these
88 Milankovitch periods from the geological record illuminate the exchange of angular momentum and
89 energy within the Earth–Moon system and the orbital evolution of the Solar System.

90 Here we report evidence for Milankovitch cycles across a ~8.7 Myr long time interval
91 in the late Cambrian. We are using high resolution (0.2 mm) XRF core scanning to investigate
92 cyclic patterns in the elemental abundances of an organic-rich, slowly deposited black shale (Alum
93 Shale) in two drill cores from southern Scandinavia. Identification of the stable 405 kyr eccentricity
94 cycle is used to construct a floating astronomical time scale and constrain the duration of late
95 Cambrian biozones and the SPICE event. The new data also constrains the Earth's precession and
96 obliquity periods and resolve the day length and Earth–Moon distance at ~493 Ma. Furthermore,
97 our cyclostratigraphic calibration allows us to reconstruct sedimentation rates that we compare to
98 changes in eustatic sea level, inferred from sequence stratigraphy.

99

100 **2 Materials and Methods**

101 **2.1 Geological setting**

102

103 The Alum Shale Formation predominantly consists of laminated, organic-rich mudstone with high
104 pyrite content. A few thin primary limestone beds occur in the middle Cambrian part (Nielsen and

105 Schovsbo, 2007), but bituminous limestone concretions and beds (so-called anthraconite or orsten)
106 are common throughout the unit and constitute up to 50% of the stratigraphic thickness in south
107 central Sweden. Limestone concretions account for 5–10% of the stratigraphic thickness in Scania-
108 Bornholm, the area in focus in the present study (southernmost Sweden and Denmark). The Alum
109 Shale Formation, which is up to ~100 m thick in Scania and ~40 m on Bornholm, was deposited
110 from the Miaolingian through earliest Ordovician (Tremadocian) in the deeper parts of an
111 epicontinental sea covering the (current) western part of Baltica. At this time, Baltica was
112 presumably located at ~30–60°S (Fig. 1A) and the Alum Shale was deposited from about the storm
113 wave base and deeper (Buchardt et al., 1997; Nielsen & Schovsbo, 2015). Sedimentary supply was
114 extremely low, reflecting that the craton was intensively peneplained, and compacted accumulation
115 rates for the Alum Shale averages 1-2 mm/kyr with maximum of 5 mm/kyr in the Southern part of
116 Scandinavia (Nielsen et al., 2018). Reworking caused by lowering of the storm wave base during
117 sea level lowstands occurred repeatedly in the paleo-inboard part of the Alum Shale basin (south
118 central Sweden), but generally are not seen in Scania-Bornholm, representing the deepest part of the
119 basin (Nielsen & Schovsbo, 2015). Deposition took place under predominantly euxinic conditions
120 and the shale is renowned for its high content of syngenetically enriched redox sensitive elements,
121 including Mo, U, and V (Dahl et al., 2019, and references therein). Nonetheless, bottom-water
122 oxygenation occurred episodically and the shale is rich in fossils, notably trilobites. Nine
123 superzones, subdivided into 31 biozones, are defined for the Miaolingian–Furongian interval in
124 Scandinavia, providing a high-resolution stratigraphic framework for study of the Alum Shale (Fig.
125 1D) (for review, see Weidner & Nielsen, 2014; Nielsen et al., 2020).

126

127 **Figure 1 here**

128

129 The present study focuses on the Miaolingian–Furongian boundary interval in two drill cores from
130 southern Scandinavia, namely Fågeltofta-2 (Få-2), and Billegrav-2 (Bi-2) (Fig. 1). The studied
131 interval spans the *A. pisiformis* Zone (Miaolingian) and the *Olenus* and *Parabolina* Superzones
132 (Furongian) in both cores, and continues further up into the *Leptoplastus*, *Protopeltura* and *Peltura*
133 Superzones in the Bi-2 core. For remarks on the informal terms ‘lower’ and ‘upper’ *Olenus*
134 Superzone, see Nielsen et al. (2020). The cores have been kept as intact as possible and no further
135 splitting has been undertaken in the search for fossils. Correlation is facilitated both by
136 identification of characteristic fossils, incidentally exposed on the surfaces of broken core pieces,
137 and the gamma ray logs recorded in the drill-holes. [The stratigraphic framework for Bi-2 are](#)
138 [described in Nielsen et al \(2018\), and we list first and last fossil appearances for Få-2 along with the](#)
139 [selected boundaries based on GR log data comparison to three other cores \(see details in Table S4\).](#)

140 The Få-2 and Bi-2 wells were drilled in 1997 and 2010, respectively. Since then, the
141 cores have been stored at the Natural History Museum of Denmark (Få-2) and the Geological
142 Survey of Greenland and Denmark (Bi-2). Both cores had a patchy white coating on their surfaces
143 (presumably a sulfate mineral resulting from incipient break down of pyrite), which was thoroughly
144 washed off using demineralized water prior to XRF analysis.

145

146 **2.2 Core scanning**

147 The elemental composition of the cores was analyzed using an Itrax X-Ray Fluorescence (XRF)
148 core scanner from Cox Laboratories at the GLOBE Institute, University of Copenhagen. The core
149 recovery is close to 100% and overall, the cores are intact so that successive core pieces easily can
150 be fitted together. The core pieces were assembled using a Cl-rich dough, allowing gaps to be easily
151 identified by XRF and removed from the analyzed signal (see details in the supplementary
152 information, SI). The core scanner is equipped with a rhodium tube as the X-Ray source. Scanning

153 was done at a vertical resolution of 0.2 mm for 7 seconds per analysis with a voltage and current on
154 the Rh-tube of 30 kV and 50 mA, respectively. Scanning was performed on the outer, round surface
155 of the drill cores (diameter of 55 mm) that exceeds the width of the scanned area of 10 mm. The
156 XRF signal was recorded with the “CoreScanner 8.6.4 Rh” software and the XRF signal was
157 converted to elemental concentrations using Q-spec with USGS SGR-1 (Green River Shale) as
158 reference material. A total of 26 and 28 different elements were measured in Få-2 and Bi-2,
159 respectively. A detailed description of quality control measures is provided in the SI.

160

161 *2.2.1 Data processing*

162 As a first step, we removed high frequency noise and detrended the signal of the element of interest.
163 To remove high frequency ($>0.5 \text{ mm}^{-1}$) noise from the elemental signal, the elemental data were
164 first smoothed using the “loess” function in Matlab with a window of 25 points corresponding to ~5
165 mm weighed smoothing (i.e. likely ~2 kyr on average). This procedure reduces noise from the
166 analyzed signal with only minimal risk of overlooking Milankovitch cycles that operate over longer
167 time scales. This translates into a longer exposure time (175 s) sufficient for detection of Mo and
168 major elements relevant in this study (see details in the SI). Diagenetic limestone intervals were
169 identified both visually and chemically and omitted from the cyclostratigraphic analysis based on
170 the assumption that they represent very short time (see discussion in section S1.5). In total, these
171 intervals accounts for 8.0% (1.7 m) and 1.4 % (0.23 m) of the studied stratigraphy in Få-2 and Bi-2
172 core, respectively (see Fig. S3). This step has only minor effects on our results, as discussed in
173 section 4.2. As remarked above, broken core pieces were assembled using a Cl-rich dough,
174 allowing gaps to be easily identified and removed from the data set (see SI for details). Long-term
175 trends were removed from the elemental data (detrended); for example: a third and a tenth-degree
176 polynomial were fitted to the sulfur data to produce detrended S signals for Få-2 and Bi-2,

177 respectively (see Fig. S3 for details).

178

179 *2.2.2. Time series analysis*

180 The detection of Milankovitch cycles was performed in a series of steps. First, stratigraphic cyclic
181 variations in the sulfur data and other elements were studied using both wavelet and the multi-taper
182 method (MTM) spectral analysis (Thomson, 1982). We performed the MTM spectral analysis using
183 Matlab's 'pmtm' function, where number of tapers = $2 \cdot nw - 1$, nw = time-halfbandwidth = 2.5, and
184 $nfft$ = number of points in the discrete Fourier transform = number of data points in the discrete data
185 series. For the wavelet analysis we used continuous 1D wavelet transform (the 'cwt' function in
186 Matlab) with the 'bump' wavelet. The significance of the periods identified in the MTM analyses
187 was determined against "the bending power law" (BPL) and the "Auto Regressive Moving
188 Average" (ARMA) as noise model (Vaughan et al., 2011). These noise models have been
189 considered as more robust than the typical autoregressive AR(1) model often favored in
190 cyclostratigraphic studies (Vaughan et al., 2011) (Fig. S4). Confidence levels (CL) for the MTM
191 were calculated using the method of Mann & Lees (1996). The identified cycles were isolated using
192 Taner band-pass filtering (Taner et al., 1979). In this way, the "filtered output" shows the
193 Milankovitch-forcing of each of the dominant modes.

194 To verify that the dominant periods in the observed signal could be forced by
195 Milankovitch-driven solar insolation, we compared the frequency ratios of the dominant modes to
196 the theoretically predicted ratios for the late Cambrian according to Milankovitch theory (Waltham
197 2015).

198 The floating age model and sedimentation rates were obtained by identifying maxima
199 of the 405 kyr eccentricity cycle (E_{405}). The final age model was constrained by simultaneous
200 correlation of biozones, stratigraphic Mo curves, and counting E_{405} cycles in the filtered outputs in

201 the two cores. The Mo curves correlate well with the gamma-log pattern, but provide a much higher
202 stratigraphic resolution. All data presented in the time domain were calibrated to a smoothed
203 version of 405 kyr derived sedimentation rates using a polynomial fit (Fig. 6A). This is done to
204 prevent abrupt shifts in the sedimentation rate across the anchored 405 kyr eccentricity maxima
205 (Fig. 6A, black curves). Further, we used the automated eCOCO algorithm to confirm that our
206 sedimentation rate curves are correct (Fig. 6A, grey circles; Li et al., 2019). The obtained floating
207 astronomical time scale was anchored at the ~497 Myr date for the Miaolingian/Furongian
208 boundary (Peng et al., 2012). Cyclic amplitude modulations in precession cycles were tested using
209 Taner band-pass filtering and Hilbert transformation (Taner et al., 1979).

210

211 **2.3 Carbon isotopes**

212

213 The carbon isotope composition and total organic carbon content were measured in 48 and 79 Alum
214 Shale samples taken from the Bi-2 and Få-2 cores, respectively. Samples of ~1–3 g were collected
215 from the cores and powdered in an agate mortar. Homogenized portions of powder (~20 mg) were
216 loaded into tin capsules, then acid fumigated with 12 M HCl and dried to remove inorganic carbon
217 and remaining water. Subsequently, the total organic carbon content and the $^{13}\text{C}/^{12}\text{C}$ ratios were
218 analyzed at the University of Copenhagen using an elemental analyser (CE1110, Thermo Fisher
219 Electron, Milan, Italy) coupled in continuous flow mode to a Finnigan MAT Delta PLUS isotope
220 ratio mass spectrometer (Thermo Fisher Scientific, Bremen, Germany). For calibration, we used a
221 pure CO_2 gas calibrated against a certified ^{13}C -sucrose (IAEA, Vienna, Austria). For quality
222 control, we used certified reference materials of loamy soil (calibrated by Elemental Microanalysis,
223 Okehampton, UK). The reproducibility of reference material analyses was $\pm 0.08\%$ (SD).

224

225 **3 Results**

226 **3.1 Identification of elemental cycles**

227

228 The Alum Shale lithology is very monotonous and exhibits no visible signs of cyclicity (Fig. 1C),
229 and appears, at first glance, a poor choice for cyclostratigraphic analyses. However, the slow
230 undisturbed deposition results in an excellent cyclostratigraphic record. The elemental XRF data
231 show pronounced cyclic patterns in the sulfur content in both cores (Fig. 2). Other elements,
232 including clay-bound elements (Si, Al, Ti, K), carbonate (Ca, Mn) and redox sensitive elements
233 (Mo, U, V), also exhibit cyclic patterns, although not as well-defined as the sulfur. Therefore, we
234 focus our cyclostratigraphic analysis on the detrended S signal.

235 **Figure 2 here**

236

237 3.1.1 Fågeltofta-2 (Scania, Sweden)

238 Several distinct cycles are recognizable in the MTM spectrum of the detrended S signal from the
239 Få-2 core (Fig. 2A), including ~ 1.6 m ($p < 0.01$), ~ 0.44 m ($p \sim 0.06$) and some shorter cycles with a
240 thickness of around ~ 0.13 m ($p < 0.01$). The ratios between these frequencies fit with the predicted
241 Milankovitch periods for the Cambrian (Waltham, 2015). If we ascribe the ~ 1.6 m cycle to the 405
242 kyr eccentricity cycle, then the ~ 0.44 m and ~ 0.13 m cycles would roughly correspond to ~ 100 kyr
243 short eccentricity and ~ 32 kyr obliquity cycles, respectively. Below, we further verify this choice
244 with independent data from Bi-2 and an age model that fits all available chemo, chrono- and
245 biostratigraphic data. Furthermore, we confirmed this interpretation using the Bayesian inverse
246 method called 'TimeOpt' (see Fig. S8 for details, Meyers 2015).

247 The 405 kyr (~ 1.6 m) eccentricity cycle is expressed throughout most of the Få-2 core,
248 but disappears in the upper *Olenus* Superzone between ~ 74 to 78 m (Fig. 2C). Likewise, the ~ 100

249 kyr (~ 0.44 m) eccentricity cycle is expressed through most of this core, but is absent in the lower
250 *Olenus* Superzone. In the *Parabolina* Superzone at ~ 69 to 71 m, the ~ 100 kyr eccentricity cycles
251 appear as two cycles with periods of ~ 0.5 and 0.35 m, which could correspond to ~ 95 and 123 kyr,
252 consistent with the ~ 100 kyr eccentricity cycles (Waltham, 2015). The wavelet spectrogram (Fig.
253 2D) shows that the ~ 32 kyr (~ 0.13 m) obliquity cycle is present with high amplitude in most of the
254 Få-2 core whereas the 18 kyr (~ 0.07 m) precession cycle is distinguishable only in the lower *Olenus*
255 Superzone, where the precession period varies stratigraphically in parallel with the obliquity cycle.
256 This parallel behavior is reflecting a variable sedimentation rate and is the reason why the
257 precession and obliquity cycle cannot be distinguished from each other in the MTM spectrum (Fig.
258 2A). Thus, a refined time scale with more precise estimates of the Milankovitch periods can be
259 obtained by taking the variable sedimentation rates into account (see section 3.3. for analyses in
260 time domain).

261

262 3.1.2. Billegrav-2 (Bornholm, Denmark)

263 One significant mode with a period of ~ 0.7 m ($p < 0.05$) is dominant in the MTM spectrum of the
264 detrended S signal from the Bi-2 core (Fig. 2B). The wavelet analysis (Fig. 2D) reveals that higher
265 frequency cycles are also expressed with periods of ~ 0.23 m and ~ 0.06 m (Fig. 2D). The ~ 0.17 m
266 period is present in the *A. pisiformis* Zone, the upper *Olenus* and the *Peltura* Superzones, and the
267 ~ 0.06 m period cycles are recognizable in shorter intervals from the mid *Olenus* Superzone to the
268 end of the *Peltura* Superzone. Figure 2D also shows that the ~ 0.7 m cycle is expressed from the
269 lower *Olenus* Superzone to the top of the studied interval (~ 103 – 114 m), but is absent in the *A.*
270 *pisiformis* Zone.

271 If the 0.7 m cycle corresponds to the 405 kyr eccentricity cycle, then the ~ 0.17 m and
272 ~ 0.06 m may correspond to the ~ 100 kyr eccentricity and the 32 kyr obliquity cycles consistent

273 with the expected Milankovitch periods for the Cambrian (Waltham, 2015).

274

275 **3.2 Age model**

276 A floating astronomical time scale for the late Cambrian was established by calibration the signal to
277 the stable 405 kyr eccentricity cycles (Fig. 3). In total, we identify thirteen 405 kyr eccentricity
278 cycles in Få-2 and twenty-one complete cycles in Bi-2. Correlation is constrained by trilobite and
279 gamma log stratigraphy, as well as Mo trends, and there is a good match between the two cores
280 regarding the eight cycles identified in the *Olenus* Superzone (Fig. 3). Five well-expressed E₄₀₅
281 cycles are recognized in the *Parabolina* Superzone of the Få-2 core and four in the Bi-2 core, where
282 a cycle thus seems to be missing. Cycles Pa-4 and Pa-5 can be recognized in both cores, which
283 leaves Pa-1, Pa-2 or Pa-3 as candidates for the missing cycle on Bornholm. The E₄₀₅ filtered output
284 for these cycles also looks perturbed in Bi-2 (Fig. 3) and we interpret this as a hiatus approximately
285 spanning the duration of Pa-2. This hiatus happens to coincide with the presence of brachiopod
286 coquinas in the *Parabolina* Superzone on Bornholm (see e.g. Hansen, 1945), which could indicate
287 winnowing of Alum Shale mud associated with sea level lowstand conditions (cf. Nielsen &
288 Schovsbo, 2015). Apart from this hiatus and the Ol-7 cycle in the Bi-2 core, all E₄₀₅ cycles appear
289 well-expressed in both cores allowing for cycle counting. No obvious perturbations can be observed
290 in the two wavelet transforms suggesting absence of other significant hiatuses and/or condensed
291 intervals and it further supports our methodology with removal of anthraconite concretions prior to
292 analysis (Fig. 2, S3).

293 Because the very top of the Furongian is not included in the studied interval, we
294 cannot number our 405 kyr cycles downwards across all stages as recommended by Hilgen et al.
295 (2020) and instead we employ a downward numbering of cycles for each superzone (Fig. 3).

296

297 **Figure 3 here, 1 page width (18x14cm)**

298

299 **3.3 Analyses in time domain and amplitude modulations**

300 The duration of the dominant orbital periods can be derived more precisely by analyzing the
301 spectrum of the series calibrated to the 405-kyr eccentricity rhythm (Fig. 4). This analysis also
302 allows us to investigate potential amplitude modulations of the dominant periods (Fig. 5), which
303 helps to validate the astronomical interpretation of the observed stratigraphic cycles.

304 In addition to the 405 kyr eccentricity cycles, the Få-2 MTM power spectrum of the
305 entire studied interval (Fig. 4A) shows spectral peaks at ~32 kyr ($p < 0.01$) and ~124 kyr ($p < 0.1$).
306 In the lower part of the *Olenus* Superzone of Få-2, two peaks of ~18 kyr ($p < 0.05$) and a ~32 kyr (p
307 < 0.01) is also clearly expressed (Fig. 4C). These modes are consistent with the estimated periods of
308 the Cambrian precession (~18 kyr) and obliquity (~32 kyr), while the 124 kyr peak is close to one
309 of the two expected main frequencies (93 and 130 kyr) of the short-eccentricity band (Waltham,
310 2015).

311 In Bi-2, the MTM power spectrum of the entire studied interval (Fig. 4B) shows three
312 spectral peaks within the short-eccentricity band at 114 kyr ($p < 0.05$), 88 kyr ($p < 0.05$) and 80 kyr
313 ($p < 0.01$). An MTM spectrum focused on the upper *Olenus* Superzone interval highlights a spectral
314 peak of the obliquity cycle at ~30 kyr ($p < 0.01$) along with two spectral peaks at ~93 and ~130 kyr
315 (Fig. 4D). These modes are also consistent with the published estimates of the Cambrian obliquity
316 (~30 kyr) and ~100 kyr eccentricity (93 and 130 kyr) periods (Waltham, 2015).

317 Visualizations of specific intervals, including the *Protopeltura* and *Leptoplastus*
318 Superzones, are included in the SI.

319

320 **Figure 4 here (1/2 page width (one column) (9x22cm))**

321
322 The 18 kyr precession component expressed in the lowermost *Olenus* Superzone of the Få-2 core
323 (Fig. 4D) exhibits amplitude modulations with a characteristic period consistent with the ~100 kyr
324 eccentricity period. We calculate an average duration of 103 kyr from six cycles in the precession
325 envelope (Fig. 5).

326 We also observe a marked shift in the dominant mode of oscillations in the detrended
327 sulfur signal across the Miaolingian–Furongian boundary in the Få-2 core changing from ~32 kyr
328 cycles (obliquity) to ~18 kyr cycles (precession) (Fig. 5). This orbital shift from obliquity-
329 dominated to precession-dominated sedimentation coincides with onset of the SPICE event (Fig. 6).
330 This shift in cyclicity could not be verified in the Bi-2 core where high-frequency cycles have not
331 been identified in this interval.

332

333 **Figure 5 here (1 page width, 18x6cm)**

334

335 **3.4 Carbon isotope stratigraphy**

336 Both cores exhibit a +1.5‰ positive $\delta^{13}\text{C}_{\text{org}}$ excursion from the *A. pisiformis* Zone into the *Olenus*
337 Superzone known as the SPICE event (Fig. 6E). The Bi-2 curve is similar in magnitude and
338 absolute values to that found in the Andrarum-3 drill core, Scania, Sweden (Ahlberg et al., 2008;
339 Balslev-Clausen et al., 2013) obtained some 7 km NW of Fågeltofta. The $\delta^{13}\text{C}_{\text{org}}$ values of Få-2 are
340 ~1 ‰ lower than that of Bi-2, but the SPICE excursion displays the same magnitude and timing at
341 both drill sites (Fig. 6E). The onset of the SPICE event is difficult to determine since $\delta^{13}\text{C}_{\text{org}}$
342 steadily increases from the base of the Drumian (Ahlberg et al. 2008). Here, we consider the end of
343 the SPICE event as the level where the $\delta^{13}\text{C}_{\text{org}}$ curve return to steady values, and define the onset of
344 SPICE where the $\delta^{13}\text{C}_{\text{org}}$ curve intercepts that post-excursion level.

345

346 **4. Discussion**

347 The sulfur content varies in a cyclic manner with up to four characteristic periods observed across
348 ~5.3 and 8.7 Myr long intervals in the two late Cambrian drill cores. The ratios between these
349 periods are in good agreement with the Milankovitch theory (Waltham, 2015) suggesting that the
350 cyclic sedimentation was driven by variation in solar insolation.

351 This interpretation is corroborated by numerous observations in our data set, which we
352 discuss below. First, we estimate the duration of biozones and find they are consistent with previous
353 constraints (Section 4.1.1). Secondly, we determine the sedimentation rates in the two cores and
354 show that they also align with previous estimates and vary in parallel as expected if the sedimentary
355 supply was controlled by sea level changes (Section 4.1.3). Thirdly, we calculate the obliquity
356 period and find that it fits with available data and models for the evolution of the Earth–Moon
357 system (Section 4.2). All of these results contribute to verify that these cycles, detected in the Alum
358 Shale Formation, were astronomically forced by variation in solar insolation. We therefore consider
359 the data reported here as a robust identification of astronomically forced climate change in the late
360 Cambrian.

361

362 **4.1. Implications for the Cambrian time scale and sea level changes**

363 4.1.1. Durations of biozones

364 According to the age model (Section 3.2), the *Olenus* Superzone (Paibian Stage) spans ~8.2 and 8.5
365 E_{405} cycles in the Få-2 and Bi-2 cores, respectively (Fig. 3). From this, we estimate the duration of
366 the *Olenus* Superzone to 3.4 ± 0.2 Myr. This figure is similar to, but far better constrained than
367 previous interpolated duration of the Paibian Stage at ~3 Myr (Peng et al., 2012). The *Parabolina*
368 Superzone spans 4.8 E_{405} cycles in the Få-2 (Fig. 3) suggesting a duration of 1.9 ± 0.3 Myr (Fig. 6).
369 This duration relies on the E_{405} cycles in the Få-2 core since a hiatus appears to be present in this

370 interval of the Bi-2 core (section 3.2). Based on the Bi-2 core, we estimate a duration of the
371 *Protopeltura* and *Leptoplastus* Superzones at 0.49 ± 0.22 Myr and 0.32 ± 0.18 Myr, respectively
372 (Fig. 3 and Fig. S7, see SI for details regarding the calculation).

373 The reported uncertainties are conservative estimates that include uncertainty of the
374 biozone boundaries plus uncertainty of the peak assignments in the cyclostratigraphic signal. Based
375 on the [tight biostratigraphic constraints \(Nielsen et al., 2018, Table S4\)](#), we assume that the
376 biozones boundaries are determined with a maximal offset of 100 kyr in both cores, and that odd
377 peak shapes contribute 100 kyr uncertainty for most superzones and 200 kyr uncertainty for the
378 *Parabolina* Superzone (due to the odd shape of Pa-1 in Bi-2). In total, our biozone durations are
379 estimated to carry ~200-300 kyr uncertainty, in good agreement with the observed discrepancy of
380 the duration of the *Olenus Superzone* ($\sim 0.3 E_{405}$ kyr = ~ 133 kyr) derived from comparison of the
381 two cores.

382

383 4.1.2. Duration of the SPICE event

384 The onset of this isotope excursion is located at the base of cycle Ap-1 in the upper part of the
385 *Agnostus pisiformis* Zone. A return to the pre-excursion values, here taken to define the upper
386 boundary of the event, is seen in the middle of the Ol-2 cycle in the upper *Olenus* Superzone (Fig.
387 6). Defined this way, the SPICE event straddles $7.5 \pm 0.5 E_{405}$ cycles, and, accordingly, the duration
388 becomes 3.0 ± 0.2 Myr.

389 The SPICE event has been previously documented in both carbonate ($\delta^{13}C_{carb}$) and
390 organic carbon ($\delta^{13}C_{org}$) in marine sedimentary sequences worldwide. However, Saltzman et al.
391 (2011) demonstrated that $\delta^{13}C_{org}$ records show an increasing trend that precedes that of $\delta^{13}C_{carb}$ in
392 most investigated sections. Also, we note that anomalously low $\delta^{13}C$ values are found immediately
393 below the SPICE event in the Drumian and Guzhangian part of the Alum Shale Formation (Ahlberg

394 et al. 2008; Balslev-Clausen et al. 2013). To date, our study represents the first attempt to precisely
395 determine the duration of the SPICE excursion. We stress that the calculated duration refers to the
396 $\delta^{13}\text{C}_{\text{org}}$ excursion in the shales. Further, a clear distinction must be made between the duration of the
397 SPICE event and the duration of the associated oceanic anoxic event (Gill et al., 2011; Dahl et al
398 2014; see also Nielsen & Schovsbo 2015, fig. 10). The SPICE event records an interval with
399 anomalous high $\delta^{13}\text{C}$ values in the oceans, whereas the coinciding global expansion of anoxic water
400 masses appears to straddle a shorter stratigraphic interval (Dahl et al. 2014). It has been suggested
401 that the longer-term drop in Mo concentrations observed at the base of the Furongian represents a
402 global Mo drawdown due to expansion of anoxic water masses at that time (Gill et al. 2011). Our
403 data show that the onset of Mo drawdown coincides with the base of the *Olenus* Superzone as
404 marked by a sudden decrease in Mo, whereas a return of Mo in the middle of Ol-6 marks a
405 significant change in slope from relatively stable to increasing Mo content (Fig. 6). Accordingly,
406 these observations suggest that the interval of intensified Mo drawdown associated with expanded
407 ocean anoxia spans $2.5 \pm 0.5 E_{405}$ cycles corresponding to a total duration of 1.0 ± 0.2 Myr in the
408 earliest Furongian.

409

410 *4.1.3. Sedimentation rates and sea level changes*

411 The sedimentation rate calculated for the Få-2 core varies from 3.2 – 4.5 mm/kyr, which is about
412 twice of the 1.3 to 2.2 mm/kyr calculated for Bi-2 (Fig. 6A). For both cores, reconstructed
413 sedimentation rates show a small increase across the Miaolingian–Furongian boundary, a steep
414 decline in the lower *Olenus* Superzone followed by an increase upwards through the upper *Olenus*
415 Superzone reaching a maximum near the *Olenus* – *Parabolina* Superzone boundary. The variable
416 sedimentation rates derived using the eCOCO analysis matches well with this trend for most of the
417 stratigraphy (Fig. 6A). A comparison between sedimentation rate and sea level changes shows

418 intervals of inverse correlation (Fig. 6B). Specifically, the well constrained sea level drop through
419 the upper *Olenus* Superzone is coupled to faster sedimentation at Få-2. Yet, there is no universal
420 correlation between sedimentation rates and inferred sea level.

421 This observation suggests that both study locations were closer to the sediment source
422 during lower sea level, just as should be expected. The differences in stratigraphic thicknesses
423 between Bornholm and Scania is ascribed to uplift of the Bornholm area, located closer to the edge
424 of the Baltica craton, see Nielsen et al. (2018) for details. In any case, the parallel changes in
425 sedimentation rates within the Alum basin inferred from our cyclostratigraphic analyses, might
426 open new prospects for reconstructing eustatic sea levels in the past.

427

428 **Figure 6 here**

429

430 **4.2. Obliquity period, Earth–Moon distance and length of the Cambrian day**

431 During geological time, dissipative effects in the Earth–Moon system have caused the Moon to
432 migrate away from the Earth, slowing down Earth’s rotation as well as the obliquity and precession
433 periods (Waltham, 2015). Our new constraint on Earth’s obliquity period in the early late Cambrian
434 nicely illustrates this process.

435 The best estimate of the obliquity period is obtained from a continuous interval that
436 preserves many characteristic cycles. The Jiangshanian interval (*Parabolina* Superzone) from 67.25
437 to 72.5 m in the Få-2 core spans 1.24 Myr (according to the Få-2 sedimentation rate, see Fig. 6) and
438 preserves four well-defined 405 kyr eccentricity cycles (Pa-1, Pa-2, Pa-3 and Pa-4) and 39 well-
439 defined obliquity cycles (Fig. 7).

440

441 **Figure 7 here (width: one page)**

442

443

444 Based on these data, we can calculate an average obliquity period of 31.9 ± 1.2 kyr for
445 the mid-Furongian, where the error represents the uncertainty derived from counting statistics of 39
446 obliquity cycles. We consider this as an upper estimate for the obliquity period because the removal
447 of limestone intervals (which reduced the total stratigraphic thickness by 7.95 % in this interval)
448 might induce a systematic bias. The limestone nodules contain on average ~20 % clay (Buchardt &
449 Nielsen, 1985), which implies a five-fold greater thickness for the uncompacted limestone in
450 comparison with the equivalent (compacted) shale, as the limestone cement represents a measure
451 for the original porosity. Accounting for this, we find the obliquity period was 31.4 ± 1.2 kyr at
452 ~493 Ma. This period is also consistent with an independent estimate of ~30 kyr obtained from the
453 MTM spectrum of the later Paibian interval (upper *Olenus* Superzone) from 109.4 to 113.0 m in Bi-
454 2 (Fig. 4D). Note that this ~30 kyr spectral peak carries significant uncertainty (Fig. 4D), since it is
455 mainly controlled by high amplitude obliquity cycles in a short stratigraphic interval at ~111.2 –
456 111.5 m (see Fig. 2D) well within one 405 kyr cycle (~0.7 m in Bi-2). In any case, the new precise
457 estimate of the obliquity period is perfectly consistent with previously reported values for the early
458 Paleozoic, including ~30.7 kyr at ~504 Ma (Fang et al. 2020) and ~30.6 kyr at ~465 Ma (Zhong et
459 al. 2018).

460 The Cambrian day length, Earth's axial precession, and the Earth–Moon distance can
461 be calculated from the obliquity period due to conservation of angular momentum in the Earth–
462 Moon system (Walker & Zahnle, 1986; Lowrie, 2007; Huang et al., 2020). Using the same
463 equations (see SI), we calculate an axial precession of 21.56 ± 0.57 kyr, an Earth–Moon distance of
464 $368.9 \pm 2.3 \cdot 10^6$ m, and a day length of 21.78 ± 0.29 hours in the late Cambrian (~493 Ma). Here,
465 the uncertainty is the propagated error from the obliquity estimate. These results address a long-
466 standing scientific conundrum of how the Moon has migrated away from the Earth. The lunar

467 recession has been approximately at ‘present rate’ in the past ~250 Ma (Laskar et al., 2004), but
468 was slower in the Paleozoic and Proterozoic (Fig. 8). The ‘ocean model’ in Fig. 8 predicts a
469 continuous increase in the tidal dissipation rate with time in good agreement with our Cambrian
470 constraint. Interestingly, the late Cambrian day was only slightly longer than would be the case if
471 the Earth-Moon system was resonance-stabilized by the semi-diurnal atmospheric thermal tide at
472 20.5 ± 1.0 hr, as has been suggested for most of the Proterozoic (Zahnle & Walker 1987, Bartlett &
473 Stevenson 2016). Waltham (2015) compares a range models and calculates the Earth–Moon-
474 distance and day length at 493 Ma to $371.7 \pm 6.8 \cdot 10^6$ m and 22.23 ± 0.90 hours, respectively. The
475 new data from the Alum shale matches Waltham’s model predictions with a slower the lunar
476 recession rate in the Paleozoic and provides to date the most precise empirical constraint on the late
477 Cambrian obliquity period, day length and Earth-Moon distance.

478

479 **Figure 8 here (size: width ½ page 9x6)**

480

481 **4.3. Drivers and responses to astronomically forced climate change in the late Cambrian**

482 The identification of Milankovitch cycles in the Alum Shale Formation implies that sedimentation
483 processes was affected by changes in solar insolation. Below, we discuss plausible scenarios that
484 could have controlled the sedimentary cyclicity.

485 The simultaneous analyses of multiple elements provide additional clues regarding
486 how the climatic signal was transferred to the sediments. First of all, the cyclicity is well preserved
487 in the bulk sulfur content of the Alum Shale, which is predominantly hosted in pyrite (FeS_2). There
488 is a tight positive correlation between Fe and S content (Pearson correlation coefficient $R > 0.8$,
489 Fig. S1) consistent with iron speciation data showing that almost all iron is hosted in pyrite (Dahl et
490 al., 2010; Gill et al., 2011). Further, Milankovitch cycles are also recorded in the abundances of

491 clay-bound elements, including aluminium (Al), titanium (Ti), potassium (K) and silicon (Si).
492 Importantly, these oscillations are anti-correlated with the sulfur cycles. For example, the Pearson
493 correlation coefficient between detrended Al and S content is -0.77 in the 85.00–88.62 m interval
494 of the Få-2 core where precession and obliquity cycles are well expressed (Fig. 3C, 5, and S5). We
495 note that the amplitudes of clay and pyrite oscillations are of the same order, so that one cyclic
496 variable could potentially drive cycles in the other via dilution.

497 The Alum Shale was predominantly deposited under euxinic conditions with shorter
498 intervals of oxic bottom waters (Dahl et al., 2010, 2019; Gill et al., 2011). Under these conditions,
499 reactive iron supply to the basin is the main limiting factor for pyrite formation (Raiswell &
500 Canfield, 2012). Therefore, we infer from the negative pyrite–clay correlation that reactive iron was
501 sourced independently of the clay to the basin. This could be the case either for iron transport via
502 aeolian dust and via the benthic iron shuttle (Raiswell & Canfield, 2012). As a first scenario, we
503 suggest that aeolian dust delivery to the Alum Shale sea was linked to seasonal variations driven by
504 insolation, e.g. the spread of drylands and/or changes in the Earth’s wind patterns. This concept has
505 been suggested for the orbitally-forced African Monsoon in the middle Holocene (Kutzbach and
506 Liu, 1997), where low seasonal contrast led to lower summer insolation and sea surface
507 temperature, therefore less evaporation, which combined with changes in the Earth’s wind systems
508 caused the Sahara desert to spread and increase dust supply to the Mediterranean and Atlantic
509 Ocean.

510 Alternative scenarios also exist, for example could eustatic sea level variations also
511 affect the benthic iron shuttle and pyrite deposition the Alum Shale sea. There is a positive long-
512 term (>1 Myr) correlation between pyrite content and eustatic sea level in the coress (e.g. *Olenus*
513 and *Parabolina* Superzones in Fig. S3 and Fig. 6), suggesting orbitally-forced sulfur maxima would

514 coincide with sea level maxima. If so, we predict that higher order sea level fluctuations are actually
515 superimposed on the sea level curve shown in Fig. 6.

516 As another scenario, enhanced weathering has been linked to eccentricity maxima and
517 greater seasonal contrast (Van der Zwan, 2002; Ma et al., 2011). Intensified weathering could have
518 promoted clay production in the hinterland, and clay delivery into the Alum Shale sea could
519 increase during wetter periods. Climate change also affect physical weathering associated with
520 freeze-thaw processes during colder winters. It is possible that clay deposition increased during
521 periods with high seasonal contrast (e.g. via weathering) and pyrite formation intensified during
522 periods with low seasonal contrast (e.g. via aeolian dust supply of iron) thus amplifying each other
523 in the observed anti-correlated manner. In any case, this study demonstrates the importance of
524 astronomically forced climatic changes in a putatively ice-free world and opens up new avenues for
525 understanding Earth's climate in the Paleozoic.

526

527 **5. Conclusion**

528

529 Our cyclostratigraphic analysis of the Cambrian Alum Shale in the Fågeltofta-2 and Billegrav-2
530 cores from southern Scandinavia has led to five key discoveries:

- 531 1) Milankovitch climate cycles are exquisitely recorded in the late Cambrian Alum Shale
532 Formation. An excellent match between the two investigated drill cores facilitated an
533 astronomical calibration of the early Furongian stratigraphy.
- 534 2) These results allowed us to refine the Cambrian timescale and provide durations of 3.4 ± 0.2
535 Myr for the *Olenus* Superzone (Paibian Stage), 1.9 ± 0.3 Myr for the *Parabolina* Superzone,
536 0.33 ± 0.18 Myr for the *Leptoplastus* Superzone, 0.51 ± 0.20 Myr for the *Protopeltura*
537 Superzone, and 3.0 ± 0.2 Myr for the SPICE event. The latter is defined here by trends

- 538 observed in marine $\delta^{13}\text{C}_{\text{org}}$.
- 539 3) Reconstructed sedimentation rates exhibit similar trends in the two cores and show an
540 inverse relationship to sea level changes.
- 541 4) In the mid-Furongian, the Earth's obliquity period, the Earth–Moon distance, and the day
542 length were 31.4 ± 1.2 kyr, $368.9 \pm 2.3 \cdot 10^6$ m, and 21.78 ± 0.29 hours, respectively.
- 543 5) The climate cycles are expressed in elements bound to pyrite (S, Fe) and anti-correlated with
544 elements hosted mainly in clay minerals (Al, Ti, K, Si). Plausible drivers for the cyclic
545 sedimentation include airborne dust delivery, eustatic sea level fluctuations, and/or
546 continental weathering.

547

548 **Acknowledgments**

549

550 We thank Marie-Louise Siggaard Andersen and Kurt Kjær for assistance and access to the core
551 scanner XRF facility at the GLOBE Institute, and Per Ambus (UCPH) for assistance with carbon
552 isotope analyses at the Department of Geosciences and Natural Resource Management (UCPH).
553 TWD acknowledges funding from the Carlsberg Foundation (CF16–0876) and the Danish Council
554 for Independent Research (DFR - 7014-00295). ATN and NSC acknowledge support from
555 Geocenter Grant 2015–5 and 2017–3. We thank Linda Hinnov for sharing the Taner filter Matlab
556 script at <http://mason.gmu.edu/~lhinnov/cyclotools/tanerfilter.m> (date: 16.03.2020).

557

558

559

560 **Author contributions:**

561 ALS and TWD designed the study. ATN and NHS provided the drill cores for analyses. ALS, TWD
562 and ZZ collected the data. ALS developed the algorithms used for XRF core scanner data reduction
563 and performed the cyclostratigraphic analysis under supervision of NT and TWD. ALS and TWD
564 wrote the manuscript with input from all authors.

565

566 **Competing Interests:** The authors declare no competing interests.

567

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742

743 **Figure captions**

744 Figure 1. Geological setting of the studied cores. A) Paleogeographic Map of the Furongian Earth
745 (Scotese, 2014) showing the location of Baltica where the Alum Shale was deposited at the time. B)
746 Isopach map of the Furongian Alum Shale in southern Scandinavia (thickness in meters). Modified
747 from Nielsen et al. (2020). C) Typical appearance of the Alum Shale drill core, which is black and
748 monotonous with no visual signs of cycles. Photograph taken by the XRF core scanner of a 0.55 m
749 interval of the Fågeltofta-2 core (88.07 – 88.62 m, *Agnostus pisiformis* Zone). White intervals
750 represent wax used to glue broken core pieces together prior to scanning (see supplementary
751 material for details). D) Scandinavian trilobite zonation of the stratigraphic intervals investigated in
752 the Fågeltofta-2 and Billegrav-2 cores. Abbreviations: M. – Miaolingian, G. –Guzhangian. Based
753 on Nielsen et al. (2020).

754

755 Figure 2. MTM power spectra for A) Fågeltofta-2 and B) Billegrav-2 cores with the corresponding
756 wavelet spectrograms shown in C and D. The four taper MTM power spectra of the detrended
757 sulfur content is shown with bending power low noise model and confidence levels. The “bumb”
758 wavelet is sensitive to high frequency variations in the signal (<8 kyr), so we have used a 100-point
759 smoothing to highlight the observed cycles in the wavelet spectrograms. Abbreviations: Ap=
760 *Agnostus pisiformis* Zone, Ol = *Olenus* Superzone, Pa =*Parabolina* Superzone, Le = *Leptoplastus*
761 Superzone, Pr = *Protopeltura* Superzone, Pe = *Peltura* Superzone.

762

763 Figure 3. Stratigraphic correlation of the detrended and smoothed sulfur content (blue curves), the
764 405 kyr filtered outputs (red curves), and molybdenum profile (green curve) between the
765 Fågeltofta-2 and Billegrav-2 drill cores. Each 405 kyr eccentricity cycles are named according to
766 the zone/superzone (Ap= *Agnostus pisiformis*, Ol = *Olenus*, Pa = *Parabolina*, Le = *Leptoplastus*, Pr

767 = *Protopeltura*, $Pe = Peltura$) and numbered from the youngest to the oldest according to
768 conventional astrochronology. The Mo and detrended S curves are smoothed with a window of 300
769 data points (corresponding to 60 mm) in both cores to visually emphasize the cycles and the longer-
770 term stratigraphic trends in the Mo curve. The filtered outputs of the detrended S contents have
771 Taner filter settings with centers and cut-offs at 1.4 m (1.0–2.1 m) and 0.66 m (0.5–1.0 m) for
772 Fågeltofta-2 and Billegrav-2, respectively. Grey area in Pa-2 in Billegrav-2 marks an inferred hiatus
773 and the question mark indicates the corresponding unknown correlation of Pa-2 between the two
774 cores. The Guzhangian-Paibian boundary is defined at the first appearance datum (FAD) of
775 *Glyptagnostus reticulatus* in a thick slope section in South China (Peng et al. 2012). This fossil
776 appears a few cm above the FAD of *Olenus gibbosus*, which is used to define the base of the
777 Paibian in Scandinavia. Hence, the Ap/Ol boundary is essentially equal to the base of the
778 Furongian.

779

780

781 Figure 4. Four taper MTM power spectra of the detrended sulfur time-series in frequency domain
782 (series calibrated to the 405-kyr eccentricity rhythm as shown in Fig. 3). Black vertical lines
783 represent the expected theoretical Milankovitch periods for the Earth at 497 Ma and the grey areas
784 represent uncertainties for these periods (17.0 ± 1.1 , 16.9 ± 1.1 , 19.6 ± 1.4 , 20.6 ± 1.6 , 32.6 ± 4.0 ,
785 94.9 ± 1.4 , 98.9 ± 1.5 , 123.9 ± 2.6 , 130.8 ± 2.9 and 405.6 ± 2.4 kyr based on Waltham, 2015).
786 Bending power laws are used as noise models in panel A, B and D, whereas ARMA(4,21) is used in
787 panel C. The ARMA(i,j) model parameters were determined using the Schwarz Information Criteria
788 (Schwarz, 1978) among 250 models where $i = 1, 2, \dots, 10$ and $j = 1, 2, \dots, 25$. CL = confidence
789 levels.

790

791 Figure 5. Amplitude of precession (red) and obliquity (black) cycles across the *A. Pisiformis-Olenus*
792 boundary showing eccentricity amplitude modulations (AM) of the precession band in the
793 Fågeltofta-2 core. The age axis is anchored at the Miaolingian/Furongian boundary set to 497.00
794 Ma (Peng et al., 2012). The black curve corresponds to the amplitude envelope of the precession,
795 and the numbers above the envelope indicate the calculated durations of each AM cycles in kyr.
796 Note the sudden switch from high amplitude 32 kyr obliquity forcing in the upper *Agnostus*
797 *pisiformis* Zone to high amplitude 18 kyr precession forcing in the *Olenus* Superzone.

798

799 Figure 6. Summary of results from the two cores. The indicated ages are anchored in the ~497 Ma
800 age estimate for the Miaolingian–Furongian boundary (Peng et al., 2012). A) The calculated
801 sedimentation rates are based on the 405 kyr eccentricity cycles (black dotted lines on Fig. 3). The
802 red and blue curves represent 10th and 18th degree polynomial fits to the sedimentation rates in the
803 Fågeltofta-2 and Billegrav-2 cores, respectively. Sedimentation rates are also calculated using the
804 eCOCO algorithm (grey circles) with default settings and theoretical astronomical periods at 1,925
805 Ma (Berger89 solution) with a sliding stratigraphic window size of 3 m and 4 m for Få-2 and Bi-2,
806 respectively. The algorithm utilizes a Monte Carlo approach to obtain sedimentation rates from a
807 possible range of values chosen to 0.2–0.6 and 0.01–0.3 cm/kyr for the Få-2 and Bi-2 core,
808 respectively. B) A best-estimated sea level curve obtained by smoothing the curve of Nielsen et al.
809 (2020) and reinterpreting some of the 3rd and 4th order oscillations. C) Filtered outputs of the sulfur
810 signals using a Taner filter centred at 405 kyr with cut-offs at 360 and 463 kyr. D) Molybdenum
811 content smoothed with a window of 500 data points to emphasize the longer-term stratigraphic
812 trends. E) $\delta^{13}\text{C}$ profiles of bulk organic carbon. Abbreviations as in Fig. 3.

813

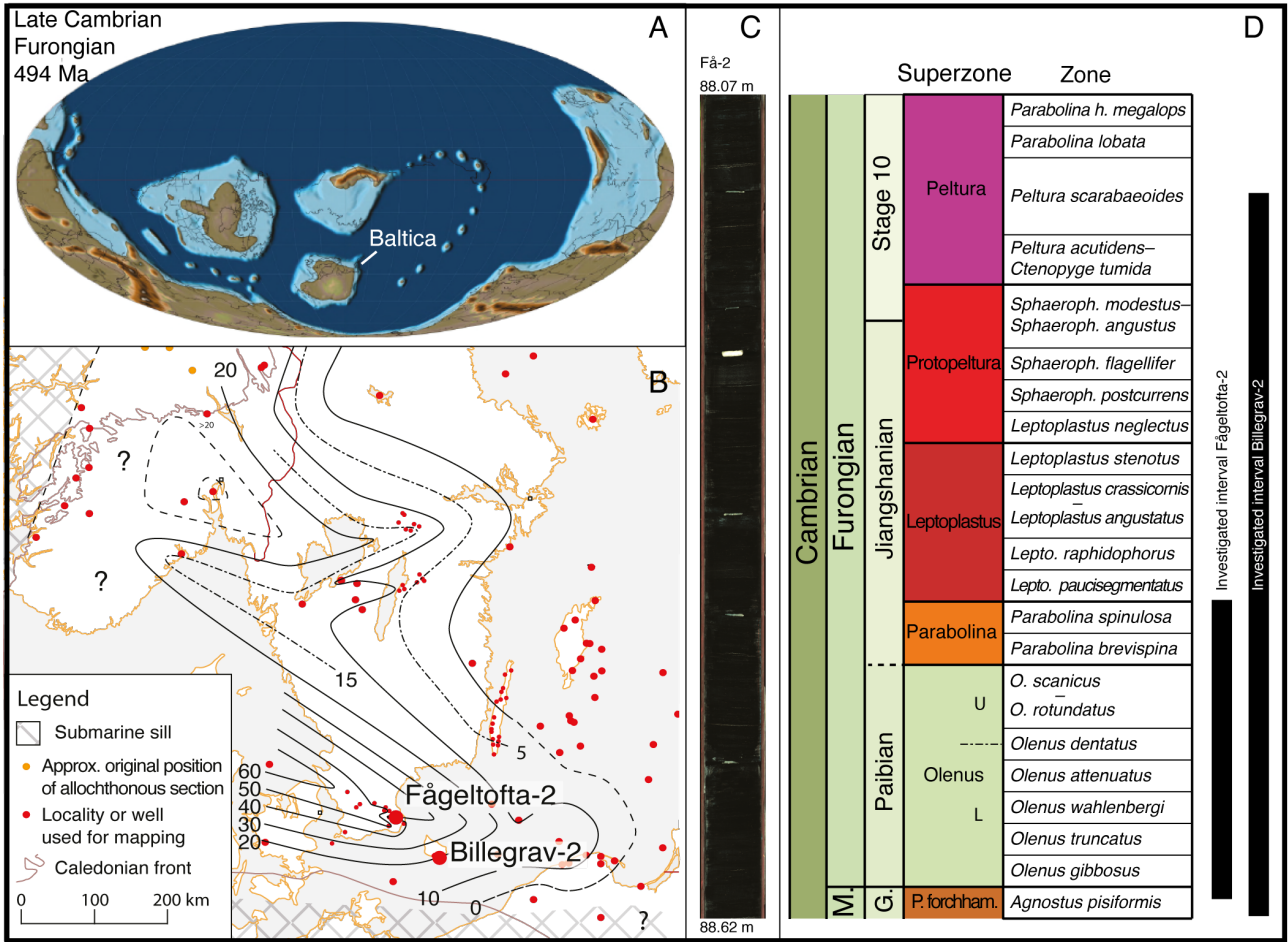
814 Figure 7. The ~32-kyr obliquity (black) and ~100-kyr eccentricity (red) cycles expressed in the
815 upper *Parabolina* Superzone of Fågeltofta-2 spanning the four 405-kyr eccentricity cycles Pa-1, Pa-
816 2, Pa-3 and Pa-4. Four taper MTM power spectra are shown for A) the detrended sulfur signal, and
817 for the same signal normalized to 405-kyr eccentricity cycles in B). Black vertical lines and grey
818 areas show the predicted Milankovitch periods and their uncertainties as in Fig. 4. The normalized
819 curve is derived by subtracting the orange curve from the blue curve in panel C. Both the 32 kyr
820 and 100 kyr periods are significant at the $P < 0.01$ level for the normalized curve. The cycles are
821 visualized in panel C with the calculated durations of each of the cycles in kyr shown on the graph.
822 CL = Confidence Level.

823

824 Figure 8. Evolution of the Earth–Moon distance over the past 1500 Myr. Present rate of tidal
825 dissipation (blue curve) and ‘Ocean model’ (purple curve) are model predictions from Waltham
826 (2015) (see equations in the SI). Here, the model parameters are chosen so that the Earth–Moon
827 distance was zero at 4.5 Ga and the characteristic timescale for changes in resonance strength is 1
828 Gyr (Waltham, 2015). Observational data from the Mansfield, Elatina, and Big Cottonwood
829 Canyon Formations are derived from tidal rhythmites (tidal bundles related to neap–spring cycles),
830 whereas data from the Walvis Ridge, Lucaogou, Xiamaling and Alum Shale Formations are based
831 on Milankovitch cycles. The uncertainty of the unit ages is smaller than the symbol size except for
832 the Big Cottonwood Canyon Formation. Tabulated data and references are summarized in the
833 supplementary material. See Fig. S9 for the same data and models plotted over the entire history of
834 the Earth.

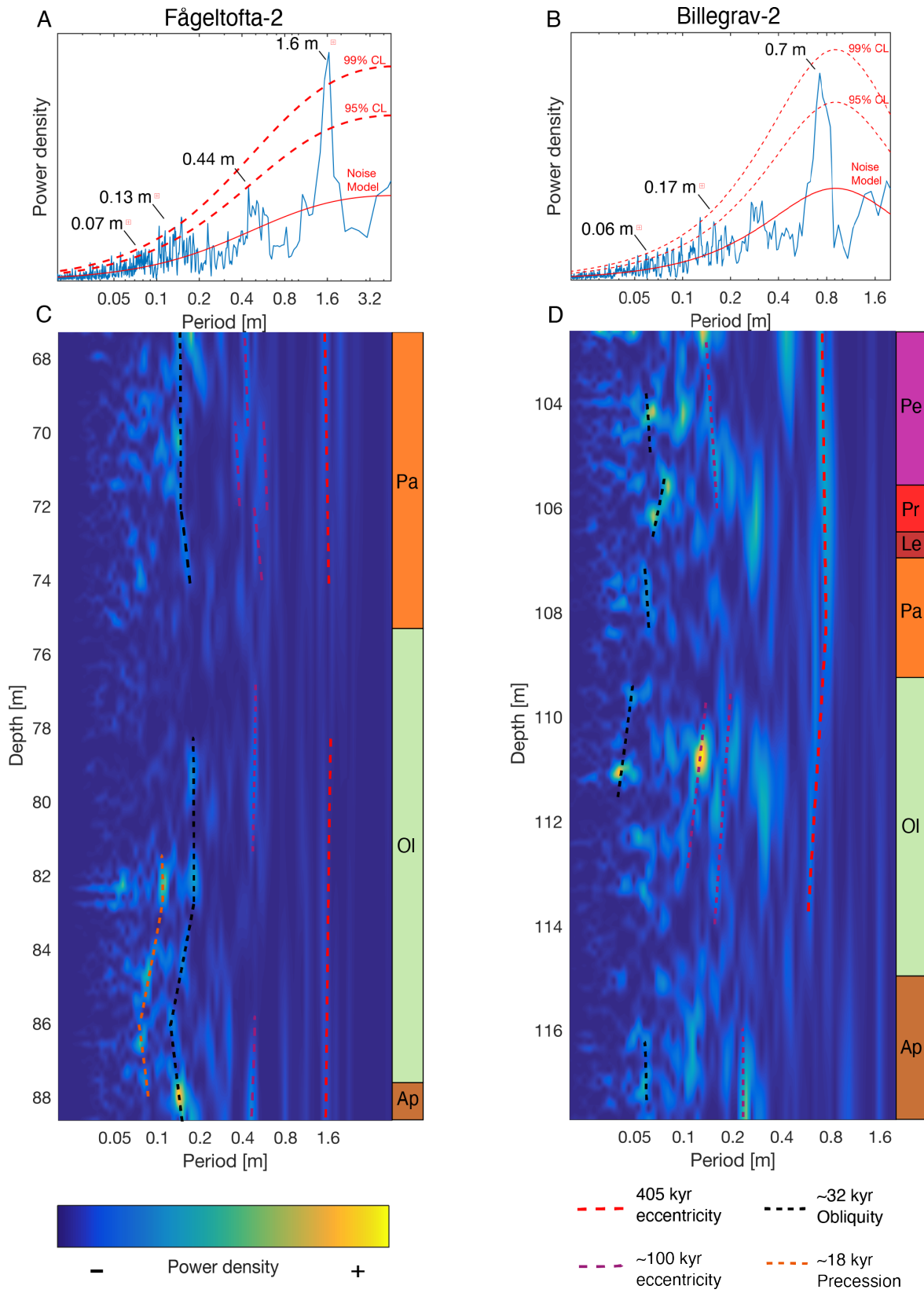
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836 Figure 1

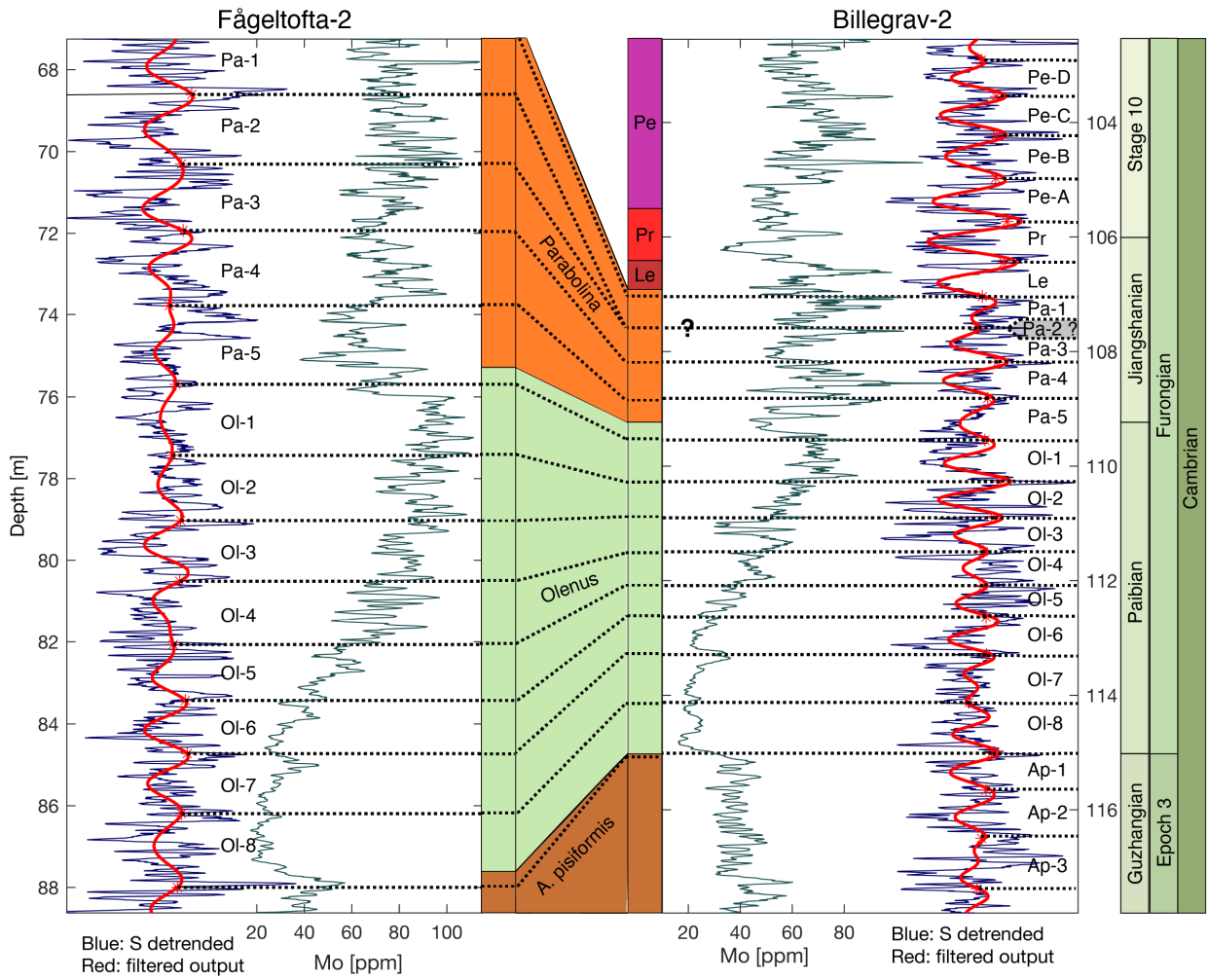


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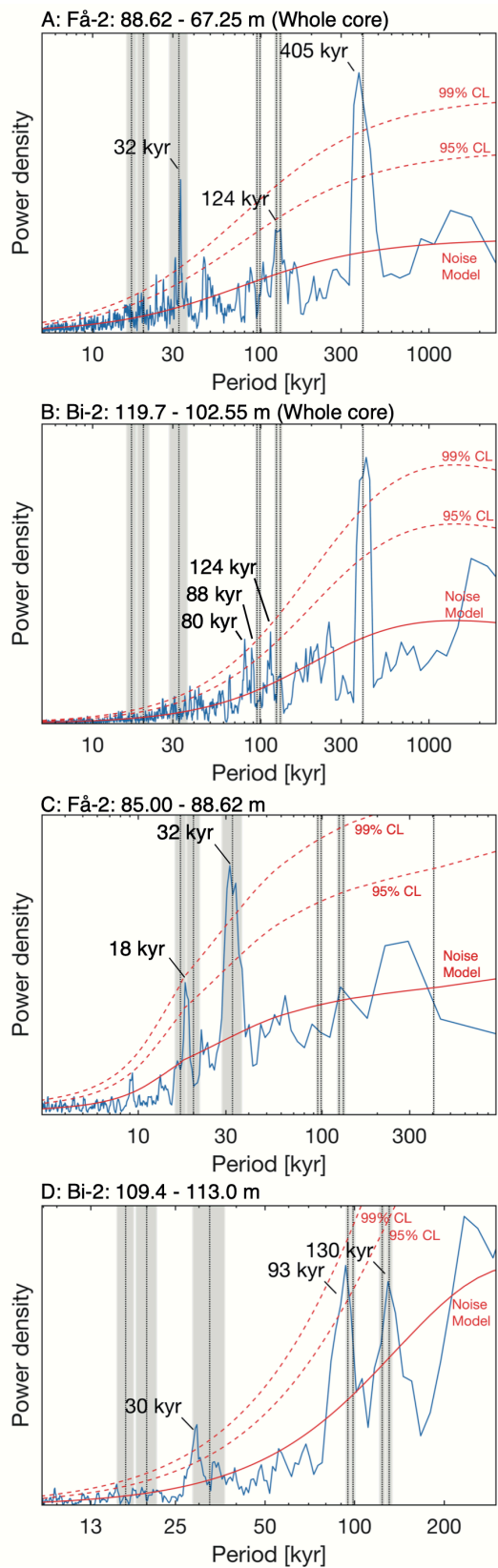
841 Figure 3



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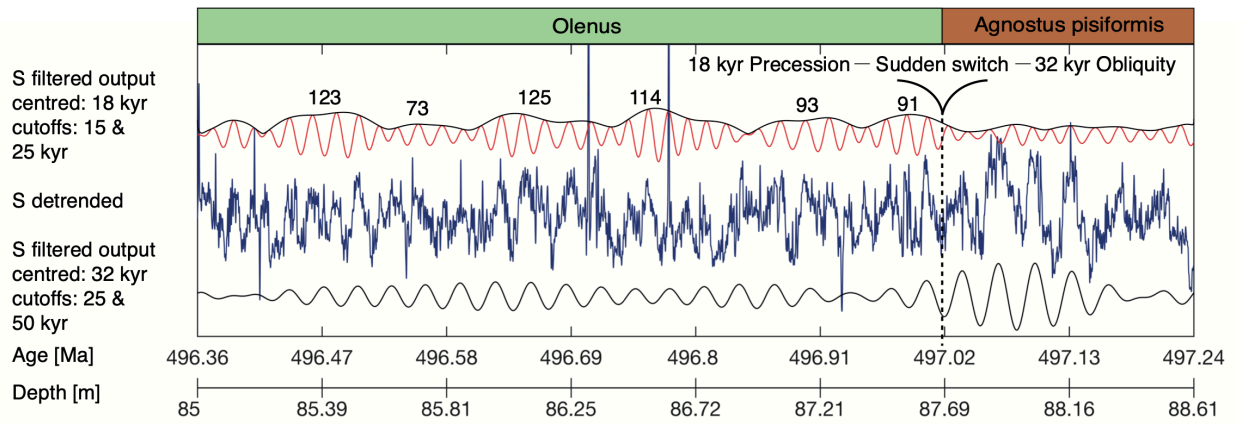
844 Figure 4



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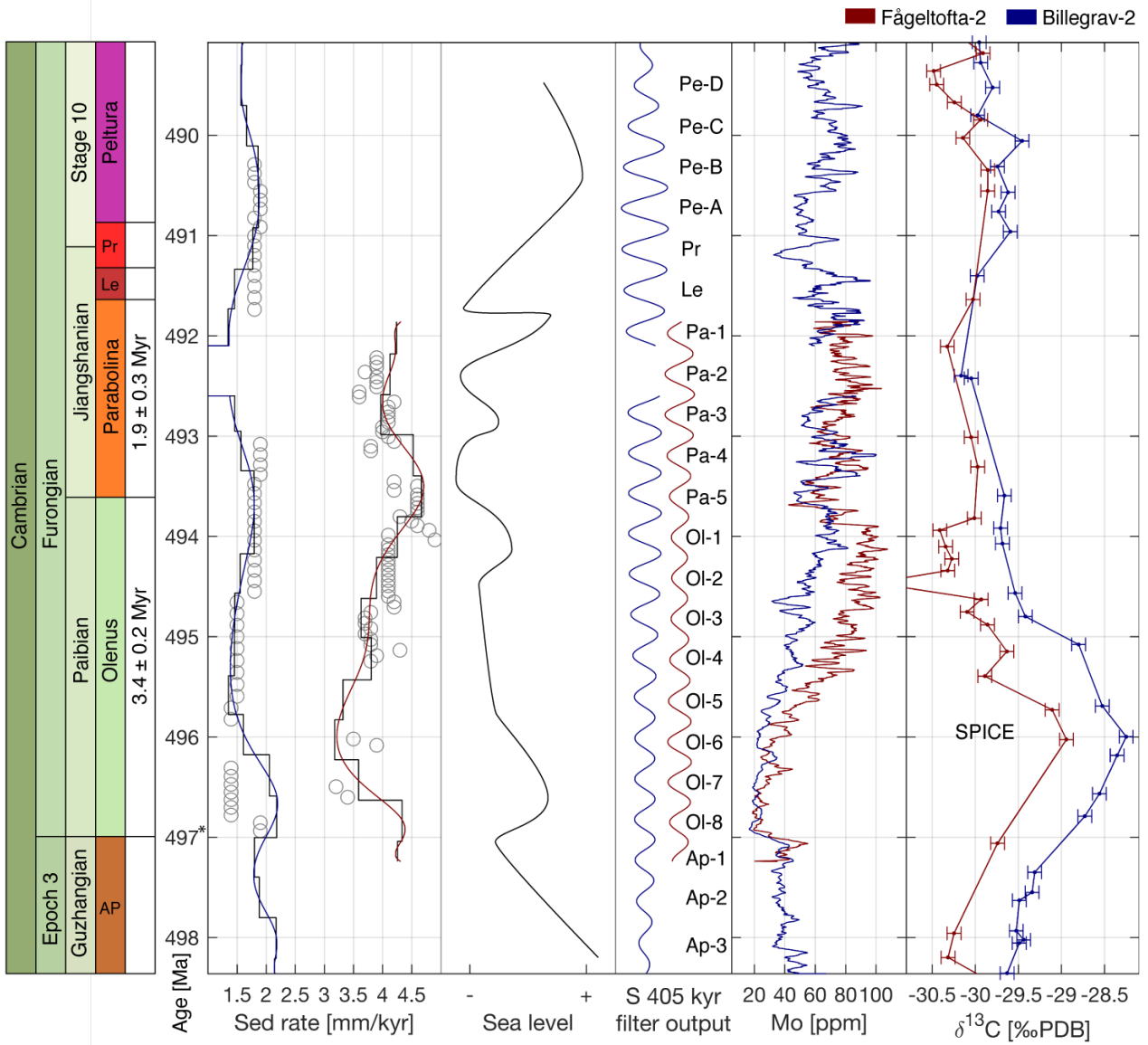
847 Figure 5



848

849

850 Figure 6



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852

